## Calculation Policy for

## Maths



Reviewed by Evelyn Orme and Jessica Emery
January 2022

|  | Language to be used |  |  |
| :---: | :---: | :---: | :---: |
| Addition | Add | Plus | Sum - the total amount resulting from the addition of two or more numbers, amounts, or item. |
|  | Total | Increase | Greater |
|  | Make | More | Altogether |
| Subtracti on | Take away | Subtract | Difference |
|  | Less | Minus | Decrease |
|  | How many left? |  |  |
| Multiplica tion | Lots of | Repeated addition | Multiply |
|  | Product - a number that you get to by multiplying two or more other numbers together. | Groups of | Multiple |
|  | Array | Times |  |
| Division | Share | Groups of | Repeated subtraction |
|  | Shared between | Split | Divide |
| Some useful vocabulary | Partition - splitting the number into smaller units e.g. tens and ones <br> Bridging - Bridging through 10 and 100 are methods that help children to add numbers mentally e.g. $9+6=15,9+1=10$ then $10+5=15$. <br> Dienes - manipulative for teaching place value and calculations. <br> Commutativity - you can swap numbers around and still get the same answer when you add or when you multiply. For example, $6+4=10$, 10-4=6. <br> Systematically - Having a pattern or order to the way you work <br> Inverse - The opposite in effect. The reverse of. <br> Integer - A number, which is not a fraction, a whole number. <br> Remainder - The number which is left over in a division in which one quantity does not exactly divide another. <br> Exchange - Regrouping means to exchange 10 of a particular place value column for 1 of the next place value columns. |  |  |

## Addition - Year 1

| Objective and Strategy | Concrete | Pictorial | Abstract |
| :---: | :---: | :---: | :---: |
| Combining two parts to make a whole: partwhole model. | Use part whole model. Use cubes to add two numbers together as a group of in a bar. | Use pictures to add two numbers together as a group or in a bar. | $4+3=7$ $10=6+4$ <br> Use the part-part whole diagram as shown above to move into the abstract. |
| Starting at the bigger number and counting on. | Start with the larger number on the bead string and then count on to the smaller number 1 by 1 to find the answer. | $12+5=17$ <br> Start at the larger number on the number line and count on in ones or in one jump to find the answer. | $5+12=17$ <br> Place the larger number in your head and count on the smaller number to find your answer. |
| Regrouping to make 10. <br> This is an essential skill for column addition later. | $6+5=11$ <br> Start with the bigger number and use the smaller number to make 10. Use ten frames. | $3+9=$ <br> Use pictures or a number line. Regroup or partition the smaller number using the partpart whole model to make 10. $9+5=14$ <br> + | $7+4=11$ <br> If I am at seven, how many more do I need to make 10 ? How many more do I add on now? $1$ |
| Represent and use number bonds and related subtraction facts within 20. | 2 more than 5 |  | Emphasis should be on the language... <br> ' 1 more than 5 is equal to 6 .' <br> ' 2 more than 5 is 7 .' <br> ' 8 is 3 more than 5.' |

## Addition - Year 2

| Objective and Strategy | Concrete | Pictorial | Abstract |
| :---: | :---: | :---: | :---: |
| Adding multiples of ten. | $50=30+20$ <br> Model using dienes and bead strings. | 3 tens +5 tens $=$ $\qquad$ tens $30+50=$ $\qquad$ <br> Use representations for base ten. | $\begin{aligned} & 20+30=50 \\ & 70=50+20 \\ & 40+\ldots=60 \end{aligned}$ |
| Use known number facts. <br> Part-part whole | $\square$ <br> Children explore ways of making numbers within 20. | $\begin{gathered} 20-\square \\ \square+\square=20 \quad 20-\square=\square \\ \square+\square=20 \quad 20-\square=\square \end{gathered}$ | $\ldots+1=16$ $16-1=\_$ <br> $1+\ldots=16$ $16-\ldots=1$ |
| Using known facts |  | Children draw representations of $\mathrm{H}, \mathrm{T}$ and O . | $3+4=7$ <br> Leads to $30+40=70$ <br> Leads to $300+400=700$ |
| Bar model | $3+4=7$ | $7+3=10$ | 23 25 <br> ?  <br> $23+25=48$  |


| Objective and Strategy | Concrete | Pictorial | Abstract |
| :---: | :---: | :---: | :---: |
| Add a 2-digit number and ones. | $17+5=22$ <br> Use ten frame to make 'magic ten.' <br> Children explore the pattern. $\begin{aligned} & 17+5=22 \\ & 27+5=32 \end{aligned}$ | Use part-part whole model and number line to model. | $17+5=22$ <br> Explore related facts$\begin{aligned} & 17+5=22 \\ & 5+17=22 \\ & 22-17=5 \\ & 22-5=17 \end{aligned}$22  <br> 17 5 |
| Add a 2-digit number and tens. | Explore that the ones digit does not $\dagger$ change. |  | $\begin{aligned} & 27+10=37 \\ & 27+20=47 \\ & 27+\ldots=57 \end{aligned}$ |
| Add two 2-digit numbers | $\left\\|_{a_{0}^{0_{0}}}^{a_{0}}\right\\| / \\|_{a_{0}}^{a_{a_{0}}}$ <br> Model using dienes, place value counters and numicon. | Use number line and bridge ten using part whole if necessary. | $\begin{gathered} t_{20}^{25+47} \\ 20+40=60 \\ 5+7=12 \\ 60+12=72 \end{gathered}$ <br> Column addition can be used to extend learning. |
| Add three 1-digit numbers | Combine to make 10 first if possible, or bridge 10 then add third digit. | representations | $\begin{aligned} (4)+7+6 & =10+7 \\ & =17 \end{aligned}$ <br> Combine the two numbers that make/bridge ten then add on the third. |

## Addition - Year 3

| Objective and Strategy | Concrete | Pictorial | Abstract |
| :---: | :---: | :---: | :---: |
| Column Addition - no regrouping (friendly numbers) <br> Add two or three 2 or 3-digit numbers. |  <br> Model using dienes or numicon. <br> Add together the ones first, then the tens. <br> Move to using place value counters. | Children move to drawing the counters using a tens and one frame. <br> The use of bar models and number lines are also used. | $\begin{array}{r} 223 \\ +114 \\ \hline 337 \end{array}$ <br> Add the ones first, then the tens, then the hundreds. |
| Column Addition with regrouping. |  <br> Exchange ten ones for a ten. Model using numicon and place value counters. | Children can draw a representation of the grid to further support their understanding, carrying the ten underneath the line. | $\begin{aligned} & \begin{array}{l} 20+5 \\ 40+8 \end{array} \\ & \hline 60+13=73 \end{aligned} \begin{aligned} & 536 \\ & \begin{array}{l} \text { Start by partitioning } \\ \text { the numbers before } \\ \text { formal column to show } \\ \text { the exchange. } \end{array} \quad \frac{+85}{621} \\ & \hline \end{aligned}$ |

## Addition - Year 4-6

| Objective and Strategy | Concrete | Pictorial | Abstract |
| :---: | :---: | :---: | :---: |
| y4-add numbers with up to 4 digits. | Children continue to use dienes or place values counters to add, exchanging ten ones for a ten and ten tens for a hundred and ten hundreds for a thousand. | $\bullet$ $\ddots 8$ $\ddots$ $\because$ <br>  $\ddots$ $\bullet$  <br> $\because$ $\ddots$ $\bullet$ $\because$ <br>  $\ddots$  $\ddots$ <br> 7 1 5 1 <br> $\bullet$ $\bullet$   <br> Draw representations using place value counters. | Continue from previous work to carry hundreds as well as tens. <br> Relate to money and measures. |
| Y5-add numbers with more than 4 digits. <br> Add decimals with 2 decimal places, including money. | As Year 4. <br> Introduce decimal place value counters and model exchange for addition. | $2.37+81.79$tens onts tents hundredty <br>  00 000 0000 g <br>   $0+$ 00 <br> 00000 0 00000 00000 <br> 000 0000   <br> 6 |  |
| Y6-add several numbers of increasing complexity. <br> Including adding money, measure and decimals with different numbers of decimal points. | As Year 5. | As Year 5. | $\begin{array}{rr} \hline 81,059 \\ 3,668 \\ 15,301 \\ +20,551 \\ \hline 120,579 \\ \hline 1111 \end{array}$ |

## Subtraction - Year 1

| Objective and Strategy | Concrete | Pictorial | Abstract |
| :---: | :---: | :---: | :---: |
| Taking away ones. | Use physical objects, counters, cubes etc to show how objects can be taken away. | $15-3=$ $\square$ <br> Cross out drawn objects to show what has been taken away. | $7-4=3$ $16-9=7$ |
| Counting back. | N <br> Move objects away from the group, counting backwards. <br> Move the beads along the bead string as you count backwards. | Count back in ones using a number line. | Put 13 in your head, count back 4. What number are you at? |
| Find the difference. | Compare objects and amounts. <br> 'Seven is 3 more than $\square$ four' <br> 'I am 2 years older than my sister' <br> Lay objects to represent bar model. | Count on using a number line to find the difference. | Hannah has 12 sweets and her sister has 5. How many more does Hannah have than her sister? |

## Subtraction - Year 1

| Objective and Strategy | Concrete | Pictorial | Abstract |
| :---: | :---: | :---: | :---: |
| Represent and use number bonds and related subtraction facts within 20. <br> Part-part whole model. | Link to addition. Use part-part whole model to model the inverse. <br> If 10 is the whole and 6 is one of the parts, what's the other part? $10-6=4$ | Use pictorial representations to show the part. | Move to using numbers within the part whole mode. |
| Make 10. | Make 14 on the ten frame. Take 4 away to make ten, then take one more away so that you have taken 5. | $\begin{array}{cc}  & 13-7 \\ 13-7-6 & -4 \\ \hline \end{array}$ <br> Jump back 3 first, then another 4. Use ten as the stopping point. | $16-8$ <br> How many do we take off first to get to 10 ? How many left to take off? |
| Bar model. | $5-2=3$ |  | 10  <br> 8 2 <br> $10=8+2$  <br> $10=2+8$  <br> $10-2=8$  <br> $10-8=2$  |

## Subtraction - Year 2

| Objective and Strategy | Concrete | Pictorial | Abstract |
| :---: | :---: | :---: | :---: |
| Regroup a ten into ten ones. | Use a place value chart to show how to change a ten into ten ones, use the term 'take and make.' | $20-4=$ | $20-4=16$ |
| Partitioning to subtract without regrouping. <br> 'Friendly numbers' | $34-13=21$ <br> Use Dienes to show how to partition the number when subtraction without regrouping. | Children draw representation of dienes and cross off. $43-21=22$ | $43-21=22$ |
| Make ten strategy <br> Progression should be crossing one ten, crossing more than one ten, crossing the hundreds. | $34-28$ <br> Use a bead bar or bead strings to model counting to next ten and the rest. | Use a number line to count on to next ten and then the rest. | $93-76=17$ |

## Subtraction - Year 3

| Objective and Strategy | Concrete | Pictorial | Abstract |
| :---: | :---: | :---: | :---: |
| Column subtraction without regrouping (friendly numbers). | Use base 10 or numicon to model. | Draw representation to support understanding. | $\begin{gathered} 47-24=23 \\ -40+7 \\ -20+4 \\ \hline 20+3 \\ \hline \end{gathered}$ <br> Intermediate step may be needed to lead to clear subtraction understanding. |
| Column subtraction with regrouping. | Being with base 10 or numicon. Move to place value counters, modelling the exchange of a ten into ten ones. Use the phrase 'take and make' for exchange. | Children may draw base ten or place value counters and cross off. |  <br> Begin by partitioning in place value counters. <br> Then move to formal method. |

## Subtraction - Year 4-6

| Objective and Strategy | Concrete | Pictorial | Abstract |
| :---: | :---: | :---: | :---: |
| Subtracting tens and ones. <br> Year 4 subtract with up to 4 digits. <br> Introduce decimal subtraction through context of money. | 234-179 <br> Model process of exchange using numicon, base ten and then move to place value counters. | Children to draw place value counters and show their exchange - see y3. | $\begin{array}{r} 26154 \\ -\quad 1562 \\ \hline 1192 \end{array}$ <br> Use the phrase 'take and make' for exchange. |
| Year 5 - Subtract with at least 4 digits, including money and measures. <br> Subtract with decimal values, including mixtures of integers and decimals and aligning the decimal. | As Year 4. | Children to draw place value counters and show their exchange - see Y3 | $\begin{aligned} & { }^{2} Z^{\prime \prime} X^{\prime} 0 \not X^{\prime} 6 \\ & -\begin{array}{r} 2128 \\ \hline 28,928 \end{array} \\ & \begin{array}{l} \text { Use zeros for } \quad{ }^{\prime} 7^{10} X^{\prime} 6^{\prime} \not \subset \cdot 0 \\ \text { placeholders. } \\ -\frac{372 \cdot 5}{6796 \cdot 5} \end{array} \end{aligned}$ |
| Year 6 - Subtract with increasingly large and more complex numbers and decimal values. |  |  | $\begin{array}{r} \circ 6816,699 \\ -\quad 89,949 \\ \hline 60,750 \end{array}$ $\begin{array}{r} 91015 \cdot 3119 \mathrm{~kg} \\ -\quad 36 \cdot 080 \mathrm{~kg} \\ \hline 69 \cdot 339 \mathrm{~kg} \end{array}$ |

## Multiplication - Year 1

| Objective and Strategy | Concrete | Pictorial | Abstract |
| :---: | :---: | :---: | :---: |
| Doubling. | Use practical activities using manipulatives including cubes and numicon to demonstrate doubling. | Draw pictures to show how to double numbers. <br> Double 4 is 8 | Partition a number and then double each part before recombining it back together. |
| Counting in multiples. | Count the groups as children are skip counting, children may use their fingers as they are skip counting. | Children make representations to show counting in multiples. | Count in multiples of a number aloud. <br> Write sequences with multiples of numbers. <br> $2,4,6,8,10$ <br> $5,10,15,20,25,30$ |
| Making equal groups and counting the total. | Use manipulatives to create equal groups. | Draw to show $2 \times 3=6$ <br> Draw and make representations. | $2 \times 4=8$ |

## Multiplication - Year 1

| Objective and Strategy | Concrete | Pictorial | Abstract |
| :---: | :---: | :---: | :---: |
| Repeated addition | Use different objects to add equal groups. | Use pictorial including number lines to solve problems. <br> There are 3 sweets in one bag. How many sweets are in 5 bags altogether? | Write addition sentences to describe objects and pictures. |
| Understanding arrays | Use objects laid out in arrays to find the answers to 2 lots of 5,3 lots of 2 etc. | Draw representations of arrays to show understanding. | $\begin{aligned} & 3 \times 2=6 \\ & 2 \times 5=10 \end{aligned}$ |

## Multiplication - Year 2

| Objective and Strategy | Concrete | Pictorial | Abstract |
| :---: | :---: | :---: | :---: |
| Doubling | Model doubling using dienes and place value counters. | Draw pictures and representations to show how to double numbers. | Partition a number and then double each part before recombining it back together. |
| Counting in multiples of $2,3,4,5,10$ from 0 . <br> (repeated addition) | Count the groups as children are skip counting, children may use their fingers as they are skip counting. Use bar models. $5+5+5+5+5+5+5+5=40$ | Number lines, counting sticks and bar models should be used to show representation of counting in multiples. | Count in multiples of a number aloud. <br> Write sequences with multiples of numbers. $\begin{aligned} & 0,2,4,6,8,10 \\ & 0,3,6,9,12,15 \\ & 0,5,10,15,20,25,30 \end{aligned}$ $4 \times 3=$ $\square$ |

## Multiplication - Year 2

| Objective and Strategy | Concrete | Pictorial | Abstract |
| :---: | :---: | :---: | :---: |
| Multiplication is commutative | Create arrays using counters, cubes and numicon. <br> Pupils should understand that an array can represent different equations and that, as multiplication is commutative, the order of the multiplication does not affect the answer. | Use representations of arrays to show different calculations and explore commutativity. <br> 0000 <br> 0000 | $\begin{aligned} & 12=3 \times 4 \\ & 12=4 \times 3 \end{aligned}$ <br> Use an array to write multiplication sentences and reinforce repeated addition. $\begin{aligned} & 5+5+5=15 \\ & 3+3+3+3+3=15 \\ & 5 \times 3=15 \\ & 3 \times 5=15 \end{aligned}$ |
| Using the inverse <br> This should be taught alongside division, so pupils learn how they work alongside each other. |  |  | $\begin{aligned} & 2 \times 4=8 \\ & 4 \times 2=8 \\ & 8 \div 2=4 \\ & 8 \div 4=2 \\ & 8=2 \times 4 \\ & 8=4 \times 2 \\ & 2=8 \div 4 \\ & 4=8 \div 2 \end{aligned}$ <br> Show all 8 related fact family sentences. |

## Multiplication - Year 3

| Objective and Strategy | Concrete | Pictorial | Abstract |
| :---: | :---: | :---: | :---: |
| Grid method | Show the links with arrays to first introduce the grid method. <br> Move onto base ten to move towards a more compact method. <br> Move on to place value counters to show how we are finding groups of a number. We are multiplying by 4 so we need 4 rows. <br> Fill each row with 126. <br>  <br>  <br> $\times 126$ <br> Add up each column, starting with the ones making any exchanges needed. <br> Then you have your answer. | Children can represent their work with place value counters in a way that they understand. <br> They can draw the counters using colours to show different amounts or just use the circles in the different columns to show their thinking as show below. <br> Bar model are sued to explore missing numbers. $4 \times \square=20$ | Relate the drawn counters method to the short multiplication method. |

## Multiplication - Year 4

| Objective and Strategy | Concrete | Pictorial | Abstract |
| :---: | :---: | :---: | :---: |
| Column multiplication <br> Move to multiplying 3 digit numbers by 1 digit. (Year 4 expectation) | Use place value counters to show how we are finding groups of a number. Fill each row with 126 . We are multiplying by 4 so we need 4 rows. <br> Children can continue to be supported by place value counters at this stage of multiplication. This initially done where there is no regrouping. $321 \times 2=642$. <br> It is important at this stage that they always multiply the ones first. <br> The corresponding long multiplication is modelled alongside. | Children can represent their work with place value counters in a way that they understand. <br> They can draw the counters using colours to show different amounts or just use the circles in the different columns to show their thinking as show below. <br> Bar modelling and number lines can support learners when solving problems with multiplication alongside the formal written methods. |  |

## Multiplication - Year 5-6

| Objective and Strategy | Concrete | Pictorial | Abstract |
| :---: | :---: | :---: | :---: |
| Column multiplication for 3 and 4 digits $\times 1$ digit | It is important at this stage that they always multiply the ones first. <br> Children can continue to be supported by place value counters at the stage of multiplication. This initially done where there is no regrouping. $321 \times 2=$ 642. | Base 10 method: <br> Grid Method: |  |
| Column multiplication | Manipulatives may still be used with the corresponding long multiplication modelled alongside. |  | $18 \times 3$ on the first row. <br> (8×3-24, carrying the 2 for 20 , then 1 <br> x 3) <br> $18 \times 10$ on the $2^{\text {nd }}$ <br> row. Show <br> multiplying by 10 by putting zero in the ones column. <br> $(1234 \times 6)$ <br> $(1234 \times 10)$ |

## Multiplication - Year 6

| Multiplying decimals up to 2 decimal places by a single digit. |  |  | Remind children that the single digit belongs in the ones column. Line up the decimal points in the question and the answer. <br> Alternatively, children can convert the number to a whole number 25.1 x 8 becomes $251 \times 8$. Then, the number would be divided to convert the answer to the correct decimal places. $251 \times 8=$ $\qquad$ divided by 10 |
| :---: | :---: | :---: | :---: |

## Division - Year 1

| Objective and <br> Strategy | Concrete | Children use pictures or shapes to share | Abstract |
| :--- | :--- | :--- | :--- | :--- |
| Division as sharing |  |  |  |
| quantities. |  |  |  |

Division - Year 2

| Objective and Strategy | Concrete | Pictorial | Abstract |
| :---: | :---: | :---: | :---: |
| Division as sharing. | I have 10 cubes, can you share them equally in 2 groups? | Children use pictures or shapes to share quantities. <br> 8 divided by 2 equals 4 . <br> Children use bar modelling to show and support understanding. <br> $12 \div 4=3$ | $12 \div 3=4$ |
| Division as grouping. | Divide quantities into equal groups. <br> Use cubes, counters, objects or place value counters to aid understanding. | Use number lines for grouping. $12 \div 3=4$ <br> Think of the bar as a whole. Split it into the number of groups you are dividing by and work out how may would be within each group $20 \div 5=?$ <br> $5 \times ?=20$ | $28 \div 7=4$ <br> Divide 28 into 7 groups. How many are in each group? |

## Division - Year 3

| Objective and Strategy | Concrete | Pictorial | Abstract |
| :---: | :---: | :---: | :---: |
| Division as grouping | Use cubes, counters, objects or place value counters to aid understanding. <br> 24 divided into groups of $6=4$ $96 \div 3=32$ | Continue to use bar modelling to aid solving division problems. $\begin{aligned} & 20 \div 5=? \\ & 5 \times ?=20 \end{aligned}$ | How many groups of 6 in 24? $24 \div 6=4$ |
| Division with arrays | Link division to multiplication by creating as array and thinking about the number sentences that can be created. <br> E.g. $\begin{array}{ll} 15 \div 3=5 & 5 \times 3=15 \\ 15 \div 5=3 & 3 \times 5=15 \end{array}$ | Draw an array and use lines to split that array into groups to make multiplication and division sentences. | Find the inverse of multiplication and division sentences by creating eight linking number sentences. $\begin{aligned} & 7 \times 4=28 \\ & 4 \times 7=28 \\ & 28 \div 7=4 \\ & 28 \div 4=7 \\ & 28=7 \times 4 \\ & 28=4 \times 7 \\ & 4=28 \div 7 \\ & 7=28 \div 4 \end{aligned}$ |

## Division - Year 3

| Objective and Strategy | Concrete | Pictorial | Abstract |
| :---: | :---: | :---: | :---: |
| Division with remainders. | $14 \div 3=$ <br> Divide objects between groups and see how much is left over. <br> Example with $40 \div 5$ <br> Ask "How many <br> Example with $38 \div 6$ | Jump forward in equal jumps on a number line then see how many more you need to jump to find a remainder. <br> Draw dots and group them to divide an amount and clearly show a remainder. <br> remainder 2 <br> Use bar models to show division with remainders. <br> ut remainder: <br> $5 s$ in $40{ }^{\circ}$ <br> ers, when it becomes inefficient to count in single $m$ corded using known facts. | Complete written divisions and show the remainder using $r$. <br> es <br> a remainder of 2 <br> tiples, bigger |

## Division - Year 4-6

| Objective and Strategy | Concrete | Pictorial | Abstract |
| :---: | :---: | :---: | :---: |
| Divide at least 3 digit numbers by 1 digit. <br> Short division | Use place value counters to divide using the bus stop method alongside. <br> Start with the biggest place value, we are sharing 40 into three groups. We can put 1 ten in each group and we have 1 ten left over. <br> We exchange this ten for ten ones and then share the ones equally among the groups. <br> We look how much in 1 group so the answer is 14 . | Students can continue to use drawn diagrams with dots or circles to help them divide numbers into equal groups. <br> Encourage them to move towards counting in multiples to divide more efficiently. | Begin with divisions that divide equally with no remainder. <br> Move onto divisions with a remainder. $$ <br> Finally move into decimal places to divide the total accurately. <br> $\frac{0663}{8 \longdiv { 5 ^ { 5 } 3 ^ { 5 } 0 ^ { 2 } 9 }}$ |

Division - Year 6


